

Finding Derivatives.

1. Find derivatives:

a) $y = \frac{2}{2x-1} - \frac{1}{x}; \quad (y' = \frac{1-4x}{x^2(2x-1)^2})$

b) $y = \arcsin x; \quad (y' = \arcsin x + \frac{x}{\sqrt{1-x^2}})$

c) $y = x^3 \ln x - \frac{x^3}{3}x \quad (y' = 3x^2 \ln x)$

d) $y = \sqrt{(x+a)(x+b)(x+c)}; \quad (y' = \frac{3x^2+2(a+b+c)+ab+bc+ac}{2\sqrt{(x+a)(x+b)(x+c)}})$

2. Find derivatives of composite functions:

a) $y = \frac{1}{3 \cos^3 x} - \frac{1}{\cos x}, \quad (y' = \frac{\sin^3 x}{\cos^4 x})$

b) $y = \sqrt{1 + \arcsin x} \quad (y' = \frac{1}{2\sqrt{1-x^2}\sqrt{1+\arcsin x}})$

c) $y = \frac{1+\cos 2x}{1-\cos 2x} \quad (y' = -2 \frac{\cos x}{\sin^3 x})$

d) $y = \frac{1}{3} \ln \frac{x^2-2x+1}{x^2+x+1} \quad (y' = \frac{x+1}{x^3-1})$

3. Find second derivatives:

a) $y = \frac{\arctan x}{1+x^2}; \quad (y'' = \frac{(6x^2-2) \arctan x - 6x}{(x^2+1)^3})$

b) $y = \frac{x}{1-x^2} \quad (y'' = -\frac{2x(x^2+3)}{(x^2-1)^3})$

c) $y = e^{-x^2} \quad (y'' = e^{-x^2}(4x^2 - 2))$